

Solutions to Old Problems in Banach Space Theory

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Abstract

We shall provide a complete answer to Lindenstrauss' Question 18 in [5].

Moreover, for a Banach space E with a Fréchet differentiable norm we shall deal with the existence of an equivalent LUR norm, a frequently asked question, see for instance [1, 2, 3, 4, 6, 7].

References

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